

Stochastic quantization of the three dimensional polymer measure

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We consider the Edwards model which describes a self-repulsive polymer. It is formally defined by

$$\nu_\lambda(d\omega) = \frac{1}{Z_\lambda} \exp(-\lambda J(\omega)) \nu_0(d\omega)$$

for $\lambda > 0$, where ν_0 denotes the Wiener measure, $J(\omega) = \int_0^1 \int_0^1 \delta_0(\omega_t - \omega_s) ds dt$ is a self-intersection local time, and Z_λ is a normalizing constant. ν_λ has been mathematically constructed for $d \leq 3$ in 1980s and it is known that ν_λ is singular with respect to ν_0 for $\lambda > 0$ when $d = 3$.

The stochastic quantization of ν_λ for $d = 2$ was studied by Albeverio, Hu, Röckner, Zhou but the case for $d = 3$ has been left. We talk about the stochastic quantization of ν_λ for $d = 3$ and mutually absolute continuity of ν_λ and $\nu_\lambda \circ \tau_h^{-1}$, where $\tau_h : \omega \mapsto \omega + h$ is a translation of a sample path ω by a continuous function h .

This talk is based on the joint work with Sergio Albeverio, Seiichiro Kusuoka, Song Liang.