

Special Lecture on Random Dynamical Systems



April 10 - 14, 2017

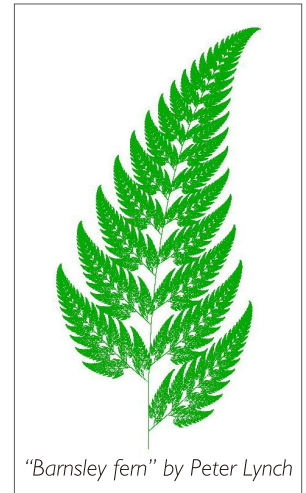
Monday, April 10	13:00-15:00
Tuesday, April 11	13:00-15:00
Wednesday, April 12	10:00-12:00
Thursday, April 13	10:00-12:00
Friday, April 14	13:00-15:00

I27 Conference Room

Faculty of Science Bldg. #3, Kyoto University

Jeroen S.W. Lamb

Kyoto University / Imperial College London



"Barnsley fern" by Peter Lynch

Dynamical systems describe the time-evolution of variables that characterize the state of a system. In deterministic autonomous dynamical systems, the corresponding equations of motion are independent of time and constant, but in random dynamical systems the equations of motion explicitly depend on a stochastic process or random variable.

The development of the field of deterministic dynamical systems – including "chaos" theory - has been one of the scientific revolutions of the twentieth century, originating with the pioneering insights of Poincaré, providing a geometric qualitative understanding of dynamical processes, aiding and complementing analytical and quantitative viewpoints.

Motivated by increasing demands on modelling from scientists, during the last decade there has been an increasing interest in time-dependent and in particular random dynamical systems, often described by stochastic differential equations. Despite the obvious scientific importance of the field, with applications ranging from physics and engineering to bio-medical and social sciences, a geometric qualitative theory for random dynamical systems is still in its infancy.

This short course consists of an introduction to random dynamical systems, from a predominantly geometric point of view. The aim is to introduce basic concepts in the context of simple examples. We will discuss some elementary results and highlight open questions.

The course is aimed at graduate students in the exact sciences. Some elementary background in dynamical systems and probability theory will be useful, but is not a strict prerequisite.

Outline

1. Barnsley's "chaos game" as a random dynamical system.
2. Random circle maps: Lyapunov exponents and synchronisation.
3. A dynamical systems perspective of stochastic ordinary differential equations.
4. Set-valued dynamical systems describing the aggregate behaviour of random dynamical systems with bounded noise.
5. A random dynamical systems perspective of critical transitions and their early warning signals.



"Lorenz model's random attractor"
by Mickaël D. Chekroun

❖ 本講義は「スーパーグローバルコース数学特別講義 2」として大学院の学生には1単位認定されます。

