

2026年 数学・数理科学グローバル講義 I (前期)

注) タイトルとアブストラクトが未定のもののみは分かり次第掲載します。

数学・数理科学グローバル特別講義1

講師: Jérémie Brioussel (Montpellier University、幾何学的群論分野)

講義日程: 2026年4月13日(月)~17日(金) 各日 13:00-15:00

タイトル: Random walks on infinite groups

概要: A random walk is the sequence of products of independent elements of a group following a given probability law. A finitely generated group can be viewed as a geometric object by means of its Cayley graph, thus a random walk is a way to explore randomly the geometry of a group. What properties of the group are reflected in the random walk? It turns out, and this is the aim of this course, that there are various connexions between characteristics of the random walk and algebraic, geometric, analytic and dynamical features of the group.

- Lecture 1: Kesten's theorem relating return probability to the Cheeger constant of isoperimetry.
- Lecture 2: Tail events and harmonic functions, entropy criterion for Liouville property.
- Lecture 3: Poisson boundary, ray criterion for identification.
- Lecture 4: Choquet-Deny groups are virtually nilpotent.
- Lecture 5: A panoramic view of finitely generated groups through the eyes of a random walker.

The course is aimed to be self-contained and will assume no specific prior knowledge.